

Theory Problems of Intelligent Control

Wen Yu

<https://www.ctrl.cinvestav.mx/~yuw/>
yuw@ctrl.cinvestav.mx

Theory Problems of Intelligent Control

- Intelligent control - 60 hours
- Theory problems of deep learning in automatic control - 60 hours
- Time series forecasting using deep learning - 60 hours

Theory Problems of Intelligent Control - 30 hours

Neural networks for control

- 1 Structure
- 2 Learning
- 3 Modeling
- 4 Control
- 5 Deep Learning

Fuzzy control

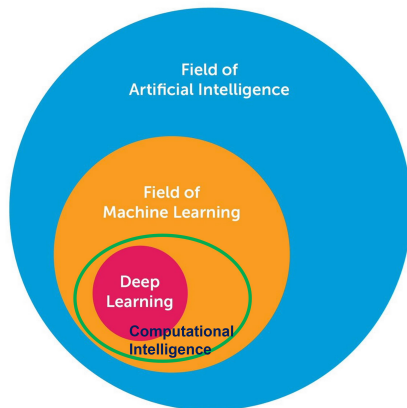
- 1 Fuzzy System
- 2 Neuro-fuzzy control

Reinforcement Learning

Content of NN

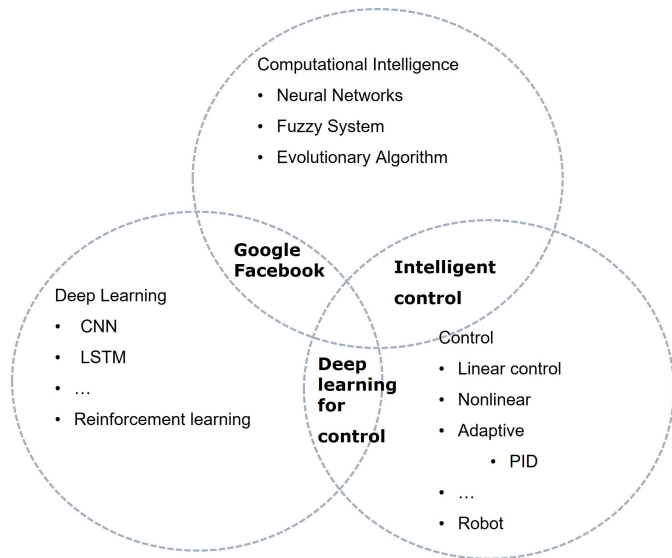
- 1 Learning methods of neural networks
- 2 Modeling and control with neural networks
- 3 Convolutional neural networks (CNN) for modeling and control
- 4 Long-short term memory (LSTM) for modeling and control
- 5 Reinforcement learning (RL)
- 6 Optimal control with RL
- 7 Time series forecasting
- 8 Time series forecasting using LSTM and CNN

Deep Learning and Artificial Intelligence

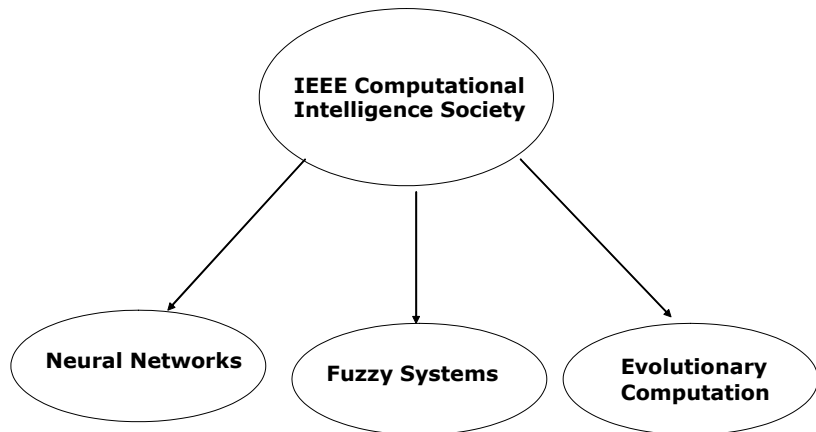


- Stuart Russell, Peter Norvig, *Artificial Intelligence: A Modern Approach*, Pearson, 4th ed, 2020

Intelligent control and Computational Intelligence



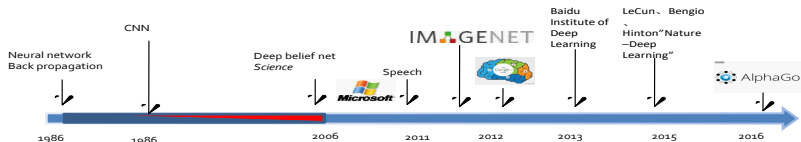
Before 2012



Intelligent control techniques include

- 1 Fuzzy system (FS)
- 2 Neural network, deep learning (NN)
- 3 Evolutionary computation (EC)
- 4 Reinforcement learning (RL)

Reinforcement learning and deep learning



- 2017. DeepMind's AI (AlphaGo) beats world's best Go player Jie Ke.



- AlphaGo improved its game after playing itself millions of times: AlphaZero
- It uses neural networks (**Deep Learning**) and **reinforcement learning**

Reference books

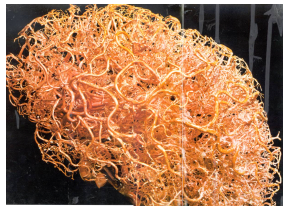
- ① Martin Hagan, ect., *Neural Network Design* (2nd Edition, 802 pages), PWS Publishing Company, septiembre 2014
- ② Li-Xin Wang, *A Course in Fuzzy Systems and Control*, Prentice Hall, Upper Saddle River, NJ, 1997
- ③ R.S. Sutton, A.G. Barto, *Reinforcement Learning: An Introduction*, 2nd edition, The MIT Press, 2018
- ④ L.Busoni, R.Babuska, Bart.Schutter, D.Ernst, *Reinforcement Learning and Dynamic Programming Using Function Approximators Technology*, CRC Press, 2010
- ⑤ Wen Yu, *PID Control with Intelligent Compensation for Exoskeleton Robots*, Academic Press, 2018
- ⑥ Simon Haykin, *Neural Networks: A Comprehensive Foundation*, Prentice Hall, 2nd Edition, 1998. *Neural Networks and Learning Machines*, 3rd Edition, Person, 2016

PROBLEMAS TEÓRICOS DEL CONTROL INTELIGENTE (28 hrs → 14)

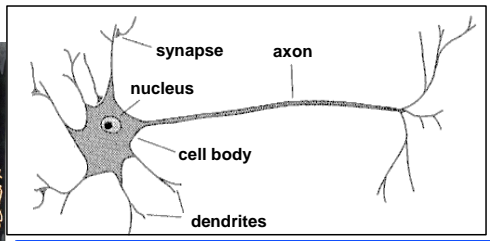


- 1 NN (6)
- 2 DL (2)
- 3 Fuzzy (3)
- 4 RL (3)

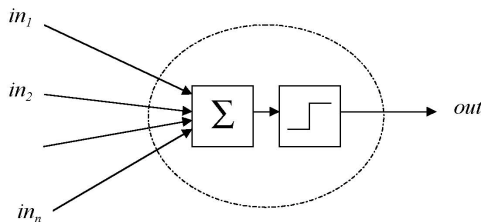
The McCulloch-Pitts Neuron



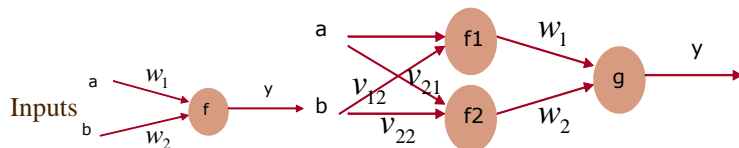
Brain



One neuron



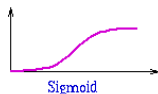
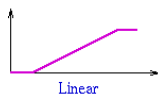
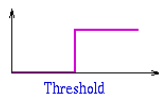
Examples



$$y = f(w_1 a + w_2 b)$$

$$y = g[w_1 f_1(v_{11} a + v_{12} b) + w_2 f_2(v_{21} a + v_{22} b)]$$

Activation functions



$$y = \operatorname{sgn}(U)$$

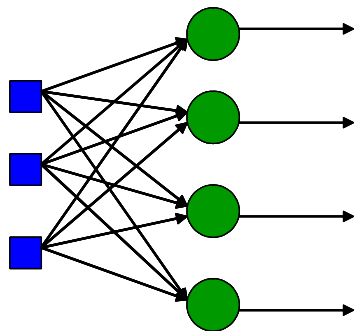
$$y = \operatorname{sat}(U), \quad y = U$$

$$y = e^{-\frac{(U-x_0)^2}{\sigma^2}}$$

$$y = \frac{a}{1+e^{-bU}} + c, \quad y = \tanh(U) = \frac{e^U - e^{-U}}{e^U + e^{-U}}$$

Perceptron

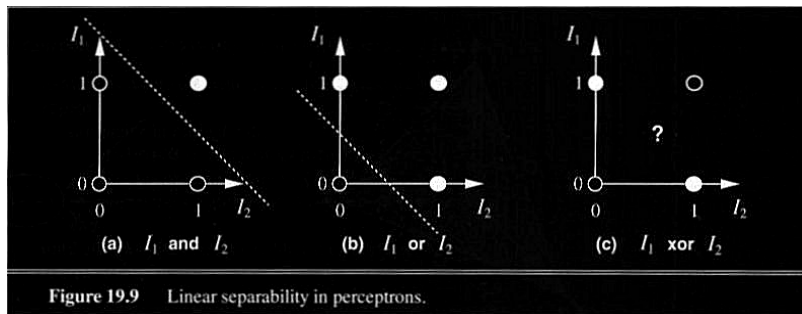
Connect any number of McCulloch-Pitts neurons together.
It is Networks of McCulloch-Pitts Neurons or *Neural Networks*



$$y_k = f_k \left(\sum_{i=1}^n W_i u_i \right), \quad k = 1, 2, \dots$$

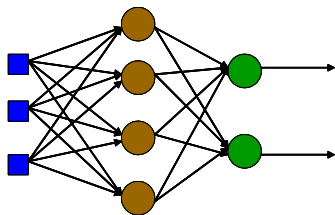
Perceptron Limitations

Linear Separability in Perceptrons

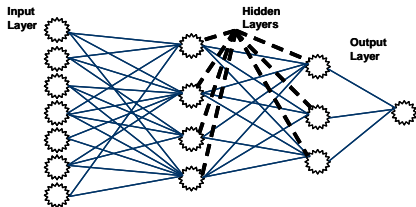


Multilayer Perceptron (MLP)

Single Layer Feed-forward : Rosenblatt's Perceptron



$$y = g \left[\sum_{j=1}^m V_j f_j \left(\sum_{i=1}^n W_i u_i \right) \right]$$



$$y(k) = \phi_p \left\{ W_p \phi_{p-1} \left[\dots W_3 \phi_2 \left\{ W_2 \phi_1 \left[W_1 x(k) \right] \right\} \right] \right\} \quad (1)$$

where $\hat{y}(k) \in \mathbb{R}^m$, $W_1 \in \mathbb{R}^{l_1 \times n}$, $b_1 \in \mathbb{R}^{l_1}$, $W_2 \in \mathbb{R}^{l_2 \times l_1}$, $b_2 \in \mathbb{R}^{l_2}$, $W_p \in \mathbb{R}^{l_p \times l_{p-1}}$, $b_p \in \mathbb{R}^{l_p}$,

The active functions are in sigmoid form,

$$\phi_i(\omega_j) = a_i / \left(1 + e^{-b_i^T \omega_j} \right) - c_i$$

where a_i , b_i , and c_i are prior defined positive constants, ω_j are the input variables to the sigmoid functions.

Or

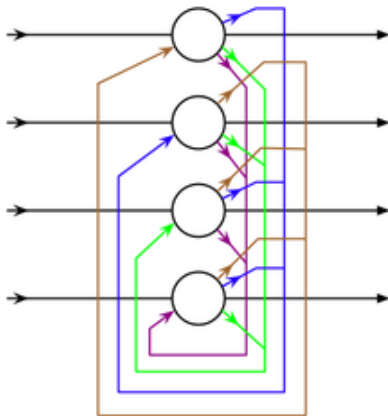
MLP (multilayer Perceptron), SVM, RBFNN, Logistic regression, Linear regression (without hidden layers)

Theorem

(Cybenko) Let activation function of neural network ϕ be a stationary, bounded, and monotone increasing. Then for any continuous functions $y = f(x)$, $x \in R^n$, and any small $\varepsilon > 0$, there exist an integer m , and real constants $W_{1,i}$ and $W_{2,ij}$, such that the neural network with ONE hidden layer satisfies

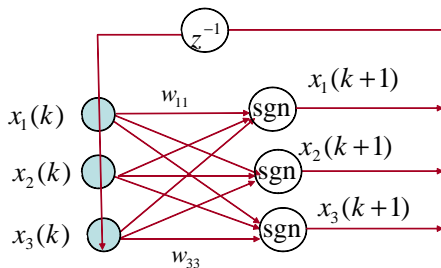
$$\left| \sum_{i=1}^m W_{1,i} \phi \left(\sum_{j=1}^n W_{2,ij} x_j \right) - f(x) \right| < \varepsilon$$

Hopfield networks (Recurrent NN)



Discrete-time Hopfield neural networks

Parallel form



$$x_i(k+1) = \text{sgn} \left(\sum_{j=1}^n W_{ij} x_j(k) + \theta_i \right), \quad \forall i$$

TEMAS SELECCIONADOS APRENDIZAJE PROFUNDO (28hrs → 14)

- 1 Wen (13/09, 20/09)
 - 2 Shengbo Hong, Eduardo Yudho (27/09)
 - 3 Suting Gao, Carlos Castillo (4/10)
 - 4 Yingqin Zhu, Victor Lechuga (11/10)
 - 5 Saul Villegas, Edson Cruz (24/10)
 - 6 Fernamdo Ramirez, Jose Padilla (31/10)
-
- Shengbo Hong, Wen (07/11)
 - Yingqin Zhu, Eduardo Yudho (21/11)
 - Wen (06/12)